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“ESTIMATION OF VIBRATION RESPONSE OF CAM AND FOLLOWER MECHANISM”

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Abstract:

In several industries so many processing machines are used. These machines are the combinations of several mechanisms .A cam and follower is one such mechanism, which used in some of these machines. If the performance of cam and follower mechanism is affected by any failure, then the total performance of the machine will be hampered. The failure in the cam and follower mechanism is caused by so many factors. One of them is the induced vibration in the mechanism itself. Hence the objective of the present work is to estimate, the vibration response of a follower for cam and follower mechanism.

1.2 THE EFFECT OF VIBRATION ON CAM AND FOLLOWER MECHANISM

A cam and follower mechanism is generally used for various applications in an industry. Efficient working of this mechanism provides better performance of machine. One probable reason for the failure of this mechanism might be induced excessive vibration. The effect of excessive vibration in of this mechanism discussed below. (a)The vibration induced in a cam body provides additional fatigue load on bearing b1 and b2 (figure 1.1 B).(b) In worst case, the cam shaft will get bent. (c) The vibration follower provides additional cycling force to a spring K. If the action of force is continued for long time then the spring get fails. (d) In worst case the follower body will get bent.

1.3: GENERAL MECHANICS OF VIBRATION INDUCED IN FOLLOWER OF CAM AND FOLLOWER MECHANISM

A cam - follower mechanism is shown in Figure 1.1. In this mechanism F is a follower, while C is a cam which rotates with uniform speed. Spring K is attached at the other end of follower. As cam C rotates with dwell period, The displacement of follower does not take place. When cam approaches for it outstroke rotation, the equilibrium of follower is being disturbed. Hence follower F moves from point a to a'. When cam approaches from its return stroke, during a rotation of a cam, the follower F moves returns down from a' to a. Thus complete one cycle of rotation of a cam provides one cycle of oscillation for follower F. If this follower motion is used for some useful work, then a process resistance can be applied to the other side of a follower. This process resistance offers at the follower end which provides a force on a cam surface through an pressure angle Φ . This force changes at every moment. Indeed, the cam also provides equal and opposite force to the follower body. This force is also time variant. During the rocking operation of a follower the follower body experiences additional forces such as (a) Inertia Force (b) Spring Force (c) Process Resistance (d) Weight. These forces are mainly responsible to induce a vibration in a follower body.



The estimation of vibration response of a follower is done like as under, For the pressing operation of rubber sheet a cam is designed by fixing the dwell period, outstroke period and return stroke period. Next to this a profile of a cam and displacement of a follower is constructed. The motion of cam is uniform acceleration and de-acceleration. The force pattern provided by cam on a follower is estimated during its outstroke and return stroke. The free body diagram (FBD) of a follower is considered for estimation of vibration of a follower. During the process of estimation, various forces has been taken into account such as (a) Inertia Force (b) Spring Force (c) Process Resistance (d) Weight. In addition to this, the load torque analysis is also done as matter of further interest.

In this case study, the operation of pressing a rubber sheet is taken. For this case, a roller follower is considered. The specifications of follower and cam is detailed as under, (a)The roller diameter is 25 cm and the length of stem is 14 cm,(b)The stem diameter is 1 cm. (c) Diameter of disc 3 cm and length 3 cm.(d)The cylinder is 5 cm. In this cylinder the rubber material is placed, which is as shown in figure 1.2



The displacement diagram and cam profile for the present study are constructed. These diagrams are shown in figure 1.3 and figure 1.4

Cam shaft diameter 40 mm. least Radius of Cam 25 mm, Diameter of Roller 25 mm, Angle of Lift or Rise 120°, Angle of Follower fall 90°, Lift of Follower 40 mm and Dwell 100 and 140°, during the lift motion is uniform acceleration and de- acceleration .

First draw the Displacement diagram

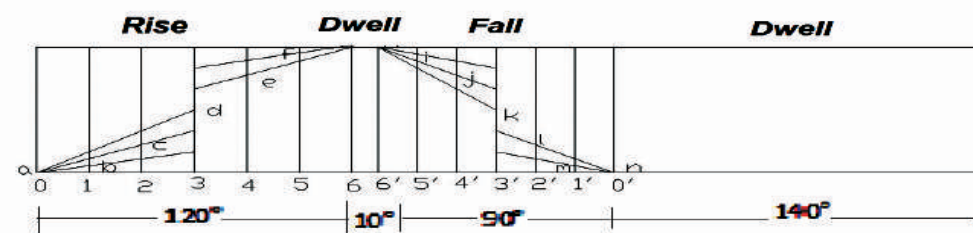


Figure 1.3: Schematic diagram the displacement of cam

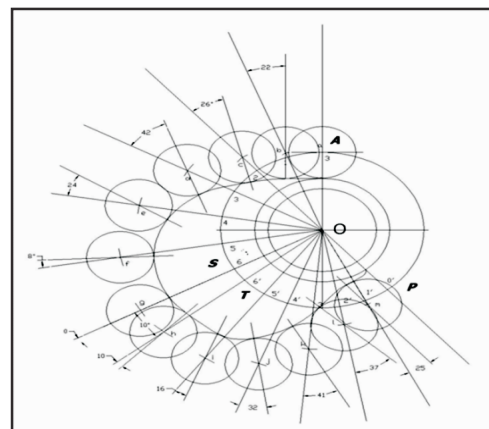


Figure 1.4: Schematic diagram of cam profile.

Figure 1.4: Schematic diagram of cam profile.

1.5: ESTIMATION OF PROCESS RESISTANCE

Procedure to calculate the process resistance is as follows,

First select the material of minimum elasticity which can easily compressed, when the follower displaces upward direction kindly see in Figure 4.1. In this case a rubber as a material for compressing is chosen.

For rubber material elasticity (E) = 110 kgf/mm² .
 $\therefore E = 11,000 \text{ Kgf / cm}^2$ (From data book)

From figure 4.1 using following parameter and calculate the process resistance is thus estimated as, the strain induced in material can be calculated by following formula.

Strain = change in length / original length = $4/5 = 0.8$;
 The original length = 5 cm, Final length = 1/4 cm;
 The corresponding stress by using following formula.
 $\therefore \text{Stress} = E * \text{strain} = 11000 * 0.8 = 880 \text{ Kgf / cm}^2$

One can estimate maximum force expressed by a stem on a rubber material by following formula

∴ Maximum force =Stresses *Area =880*0.785*9 =6217.2 kgf =6200kgf
Now ,process resistance is divided into 12 equal parts which is shown Figure 4.4

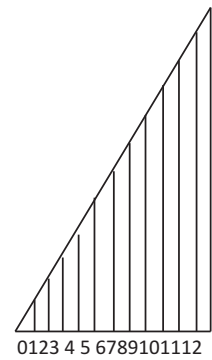


Figure1.5: Schematic diagrams for
Process Resistance

SR. NO.	Forces(kgf)
0	0
1	516.66
2	1033.32
3	1530
4	2066.66
5	2583.32
6	3100
7	3616.66
8	4133.32
9	4650
10	5166.66
11	5683.32
12	6200

Table 1.1 For Process Resistance

1.6: ESTIMATION OF VOLUME, WHIGHT OF FOLLWER,ACCLERATION AND INERTIA FORCE

With the reference to Figure 4.1, one can estimate the following parameter.(a) volume of follower.(b)Mass of follower.(c)Inertia force on a follower.(d)Acceleration of follower
Volume of follower Equation can be estimated by using below stated formula.
Volume of stem $V1=\pi/4(d)^2l=3.14/4*(1)^2*0.3=2.12$ cubic cm
Where d is diameter, l is length of stem
Volume of Disc $V2=\pi/4(d)^2l=3.14/4*(3)^2*14=10.99$ cubic cm
Volume of Hemispherical $V3=4/3 \pi(r)^3=4/3 \pi *(1)^3=4.18$ cubic cm
Where r is radius of stem
∴Total Volume of follower = $V1+V2+V3 = 2.12+10.99+4.18 =17.29$ cubic cm.=20 cubic cm.
Weight of follower calculated by following formula.
Weight of follower= $20*8$ gm/cc= 160 gms= 0.16 kgf = 1.6 N
Acceleration of a follower can be calculated as follow
 $S = ut + (1/2) at^2$
Where S is a distance travel by follower, t is a time, a is acceleration of a follower
In present case rpm of cam is a running at 300 rpm
Therefore, 300 revolution = 60 second.
∴ 1 revolution = 0.2 second = 200 millisecond.
We know that, 1 sec = 1000 millisecond.
∴For 360°revolution =200 millisecond.
∴For 60°revolution=33 millisecond.
Assume S=2 cm
∴ T=0.03 sec.
One knows that $S =Ut + (1/2) at^2$
 $0.02 =0 + (1/2) (a)*(0.03)^2$
∴ Acceleration (a)of follower= 44.44 m/s²
Inertia force calculated by following formula
Inertia Force = (W/g) X a
 $= (0.16/9.81)X 44.44$
∴ Inertia force= 0.72 kgf

1.7: CONSIDER THE FREE BODY DIAGRAM (FBD) OF FOLLOWER FOR OUTSTROKE

The follower is a converted into a free body diagram in which various forces act. When a follower moves a distance of 0-20mm during outstroke in this phase acceleration act in upward direction. While the

weight of follower, inertia force, process resistance, spring force and initial act in downward direction which is shown in figure 1.6.

(a) When follower approaches during outstroke from 0-20 mm.



Figure 1.6: Free body diagram for follower which is approaches during outstroke from 0- 20mm

From the representation of FBD one can balance the force system by following way,

Total upward force by cam on follower during the direction of travel

$$= \text{Weight} + \text{Inertia force} + \text{spring force} + \text{process resistance}$$

$$F_2(3) = 0.16 + 0.72 + K \cdot 0.5 \cdot 2 + 3100$$

Where $F_2(3)$ is a force is given by link 2 to link 3 i.e by cam on follower, k is a spring constant and x is displacement

When follower approaches during outstroke from 20-40 mm.

When a follower approaches for a distance 20-40mm, during outstroke. The inertia force act upward direction. While weight, spring force, acceleration act on a downward direction. In this case process resistance is negligible



Figure 1.7: Free body diagram for follower which is approaches during outstroke from 20-40mm.

From the representation of FBD one can balance the force system by following way,

Total upward force by cam on follower during the direction of travel =

$$= \text{Weight} + \text{Inertia force} - \text{spring force} - \text{process resistance}$$

$$F_2(3) = 0.72 - 0.16 + (-K \cdot X \cdot 0.5) - 6200/40$$

Where $F_2(3)$ is a force is given by link 2 to link 3 i.e by cam on follower.

1.8: WHEN THE FOLLOWER APPROCHES DURING RETURN STROKE FROM 40-20 MM.(?)



Figure 1.8 : Schematic of FBD for follower during return stroke

From the representation of FBD one can balance the force system by following way,

Now calculate value of spring constant (K):-

Total upward force by cam on follower during the direction of travel =

$$= \text{Weight} + \text{Inertia force} - \text{spring force} - \text{process resistance}$$

$$F_2(3) = -0.16 + 0.72 + (-K \cdot X \cdot 0.5)$$

In this condition assume, $F_2(3) = 0$

$$-0.16 - K(2) \cdot 0.5 + 0.72 = 0$$

$$-K(2) \cdot 0.5 - 0.56 = 0$$

$$\therefore \text{Spring constant } K = 0.56 \text{ kgf/cm}$$

1.9: Estimation of $F_2(3)$ for different angles of cam rotation during outstroke.

Cam rotation during outstroke (cam angle at 0°):-

When a cam is at 0° during outstroke, in this phase acceleration act upward direction. While the weight of follower, inertia force act downward in direction which is shown in figure 4.5(a). In this case spring force and resistance force is negligible



Figure 1.9: Cam rotation during outstroke(cam angle at 0°).

From the representation of FBD on can balance the force system by following way,
Total upward force by cam on follower during the direction of travel =
Weight + Inertia force + spring force + process resistance+ acceleration
∴F2 (3) = 0.72+0.16 = 0.88 Kgf.

Thus the further calculation is same as above whose answers given in table as shown for 20°,40°,60°,80°,100° and120°.

2.0: FORCE EXERTED BY CAM ON FOLLOWER ALONG LINE OF STROKE .

Thus the different force exerted at the variation of cam angle by cam on follower is in table 1.2.

ANGLE(θ)	FORCE F ₂ (3)(KGF)	PRESSURE ANGLE(Φ)	FORCE ALONG COMMON NORMAL F ₂ (3) X 1 / COSΦ
0°	0.88	0°	0.88
20°	1034.76	22°	1116.02
40°	2067.79	26°	2300.62
60°	3101.44	42°	4173.39
80°	4133.712	24°	4524.911
100°	5168.536	8.0°	5219.33
120°	6202	0°	6202

Table 1.2.Force exerted by cam on follower along line of stroke.

2.1: ESTIMATION OF LOAD TORQUE FOR CAM ROTATION DURING OUTSTROKE.

The load torque is calculated by multiplying the F2 (3) force with the length of link arm moment. Refer Figure 2.1.The values of different load torque is given in the table 2.0.

SR. NO.	ANGLE(θ)	FORCE F ₂ (3) (KGF)	LINK OF MOMENT(cm)	LOAD TORQUE(kgf-cm)
1	0°	0.88	L1=0.0	0
2	20°	1116.02	L2=1.6	1785.632
3	40°	2300.62	L3=2.0	4601.24
4	60°	4173.39	L4=3.8	15858.882
5	80°	4524.911	L5=2.8	12669.75
6	100°	5219.33	L6=0.8	4175.464
7	120°	6202	L7=0.0	0

Table 2.0: Estimation of Load Torque for cam rotation during outstroke.

[illegible]

Thus the different force exerted at the variation of cam angle by cam on follower is in table 1.4



ANGLE(θ)	FORCE F ₂ (3)(KGF)	PRESSURE ANGLE(Φ)	FORCE ALONG COMMON NORMALF ₂ (3) X 1 / COSΦ
130°	0.56	10°	0.56
145°	0.504	16°	0.5243
160°	0.308	32°	0.3631
175°	0.0	41°	0.0
190°	-0.308	37°	-0.3856
205°	-0.504	25°	-0.5561
220°	0.16	0°	0.16

Table 1.4 : Force exerted by cam on follower along line of stroke.

2.4: ESTIMATION OF LOAD TORQUE FOR CAM ROTATION DURING RETURN STROKE.

The load torque is calculated by multiplying the f3(2) force with the length of link arm moment. The values of different load torque is given in the table 1.5

SR. NO.	ANGLE(θ)	FORCE F2(3) (KGF)	LINK OF MOMENT(cm)	LOAD TORQUE(kgf-cm)
1	130°	0.56	1.13	0.63
2	145°	0.5243	2.0	1.0486
3	160°	0.3631	3.8	1.379
4	175°	0.0	3.7	0.0
5	190°	-0.3856	2.7	-1.04112
6	205°	-0.5561	1.7	-0.945
7	220°	0.16	0	0.0

Table 1.5: Estimation of Load Torque for cam rotation during return stroke.

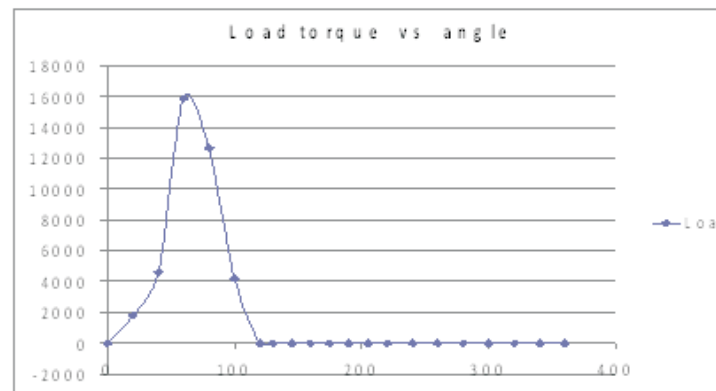
2.5: ESTIMATION OF POWER REQUIRTMENT:-

With the reference to Figure 2.3 one can estimate the power required to drive the cam shaft.
Consider Triangle A1. Portion from the graph(figure 4.12)

$A1 = 1/2 * b * h = 0.5 * 20 * \pi / 180 * 1784.768 = 311.44 \text{ kgf-cm}^2$
Trapezoidal $A2 = 1/2 * b * h + b * h = 0.5 * 20 * \pi / 180 * (4601.24 - 2816.42) + \pi / 180 * 20 * (2816.22 - 0)$
 $= 294.310 \text{ kgf-cm}^2$
Same calculation for A3, A4, A5, A6, A7, A8, A9, A10, A11 & A12 As above

$A3 = 3570.28 \text{ kgf-cm}^2$ $A4 = 4968.71 \text{ kgf-cm}^2$ $A5 = 2944.71 \text{ kgf-cm}^2$
 $A6 = 728.61 \text{ kgf-cm}^2$ $A7 = 0.2744 \text{ kgf-cm}^2$ $A8 = 0.3610 \text{ kgf-cm}^2$
 $A9 = 0.1804 \text{ kgf-cm}^2$ $A10 = -0.1362 \text{ kgf-cm}^2$ $A11 = -0.247 \text{ kgf-cm}^2$
 $A12 = -0.1236 \text{ kgf-cm}^2$
Total Area = 18549.49 kgf-cm²

$\therefore T_{\text{mean}} = \text{Total area} / \text{angle} = 18549.49 / (\pi / 180 * 360^\circ) = 2952.24 \text{ kgf-cm} = 268.89 \text{ N-m}$
Power = $T_{\text{mean}} * \omega$
Assume speed N = 120 r.p.m
power = $T_{\text{mean}} * 2\pi * N = 3639 \text{ kw}$
Now calculate Horse power
H.P. = $3639 / 786 = 4.87 \text{ hp}$
Estimate H.P. motor requirement
85% mechanical efficiency and



2.6: ESTIMATION OF FLY WHEEL REQUIRTMENT

Now calculate fluctuation of energy ΔE

From T- θ graph(Figure 4.11) calculate the total Area:-

Triangle $\Delta 1 = \frac{1}{2} \times (h \times b) = \frac{1}{2} \times (4601.24 - 2952.24) \times (40 - 28) \times \pi / 180$
 $= 172.68 \text{ kgf-cm}$

Triangle $\Delta 2 = 1964.44 \text{ kgf-cm}$

Triangle $\Delta 3 = 1112.99 \text{ kgf-cm}$

Triangle $\Delta 4 = 1407.95 \text{ kgf-cm}$

Triangle $\Delta 5 = 64.04 \text{ kgf-cm}$

Rectangle $\Delta 1 = (12699.75 - 4601.24) \times (80 - 60) \times \pi / 180 = 2826.37 \text{ kgf-cm}$

Rectangle $\Delta 2 = 1751.51 \text{ kgf-cm}$

$\therefore$ Fluctuation of energy $\Delta E = \Delta 1 + \Delta 2 + \Delta 3 + \Delta 4 + \Delta 5 + \Delta 1 + \Delta 2$

$\therefore \Delta E = 9299.98 \text{ kgf-cm} = 9.299 \times 9.81 = 91.223 \text{ N-m}$

We know that ,

Fluctuation of energy $\Delta E = I \omega^2 C_s$

$91.223 = I \times (2\pi \times 120 / 60)^2 \times 0.0225$

$\therefore$ Moment of inertia $I = 322.64 \text{ kg-m}^2$

Now estimate size of flywheel:-

Assuming mean diameter of flywheel(D_m)=0.9m

$\therefore$ Radius of gyration= $D_m / 2 = 0.9 / 2 = 450 \text{ mm}$

We know that, $I = mk^2 = 322.64 = m (0.45)^2$

$\therefore$ Weight of flywheel(m)= 1593.28 kg

Assuming cast iron of gravity 7.2(from data book p.n. 36).

$\therefore$ Density (ρ)= $7.2 \times 10^3 \text{ kg/m}^3$

Rim cross section of flywheel:-

Weight of flywheel(m)= Area * Length * Density = $A \times \pi \times D_m \times \rho$

$1593.28 = A \times 3.14 \times 0.45 \times 7.2 \times 1000$

$\therefore$ Area $A = 0.1566 \text{ m}^2$ $A = 2h^2 \therefore h = 0.279 \text{ m}^2$

If $b = 2h \therefore b = 0.5596 \text{ m}$

$\therefore$ Flywheel diameter $D_o = D_m + h = 1.45 \text{ m}$

Since the value of $D_o = 1.45 \text{ m}$.

2.7: ESTIMATION OF VIBRATION RESPONSE OF A FOLLOWER OF CAM AND FOLLOWER MECHANISM.

The estimated force F_2 (3) which is exerted by cam and follower is shown in figure 4.12

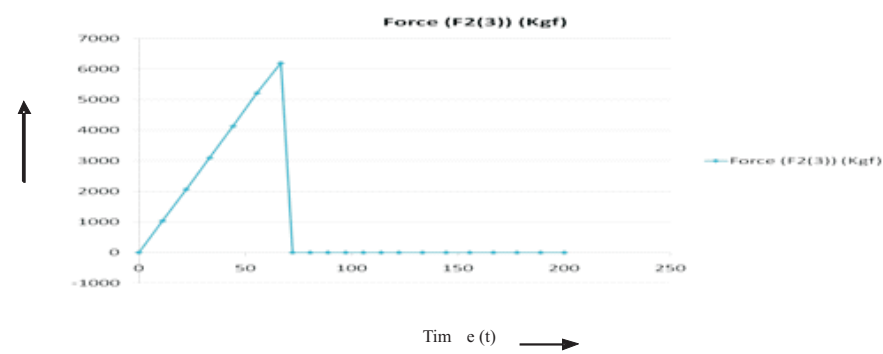
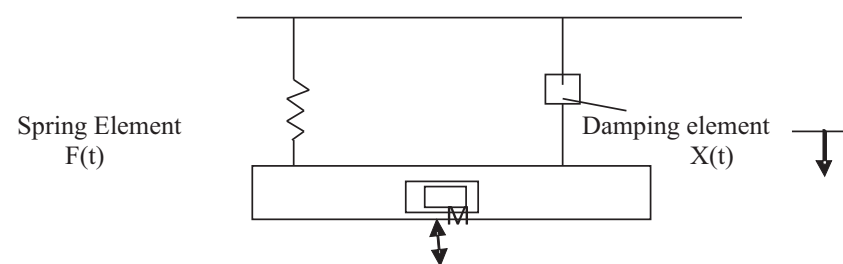


Figure 2.4: Graph between force F2(3) Vs time t.

This force pattern is now useful for estimation of vibration response of a follower. Hence in view of this the total follower structure is considered as single mass single stiffness and single damper unit (Refer Figure 2.5). The mass of follower designated as m , while stiffness is designated as K , and damper is designated as C .

The derivation of governing equations for such a system is detailed under, If the system is subjected to vertical force, say $f(t)$, then Newton's law of motion leads to the differential equation of motion in terms of the displacement as a function of time, $x(t)$



Figure(2.5): Schematic of representation of a column as a single mass degree of freedom.

$$m \frac{d^2 x}{dt^2} + c \frac{dx}{dt} + kx(t) = f(t) \quad \dots\dots\dots(1.1)$$

m =mass k =spring stiffness C =damper element

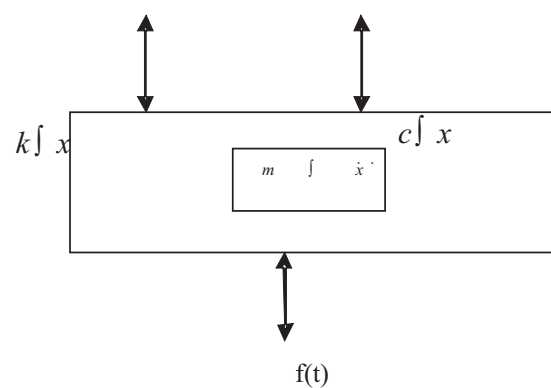


Figure 2.6: schematic of a Free body diagram.

One solution of governing equation can be obtained by following way
In many cases the vibrations are periodic like the case we are considering i.e. is the vibrations caused by

periodic excitation of follower. Here oversimplifying assumptions considered that follower experiences a periodic excitation. Any periodic function of time can be represented as an infinite sum of sine and cosine terms

If $f(t)$ is periodic function with a period t its Fourier series representation is given by

$$f(t) = \frac{a_0}{2} + a_1 \cos t + a_2 \cos 2t + \dots + b_1 \sin t + b_2 \sin 2t + \dots$$

$$= \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nt + b_n \sin nt) \quad \dots\dots\dots(1.2)$$

When $\omega = 2\pi/t$ is the fundamental frequency and $a_0, a_1, a_2, a_3, \dots, b_1, b_2, \dots$ are constant coefficient. To determine the coefficients a_n and b_n , we multiply Equation(4.1) by $\sin nt$ and $\cos nt$ respectively, and integrate over one period $\int_0^{2\pi/\omega} dt$. Then one notices that all terms except one on the right hand side of the equation will be zero and one obtain

$$a_0 = \frac{1}{\omega} \int_0^{2\pi/\omega} f(t) dt = \frac{2}{\omega} \int_0^{2\pi/\omega} f(t) dt \quad \dots\dots\dots(1.3)$$

$$a_n = \frac{1}{\omega} \int_0^{2\pi/\omega} f(t) \cos n\omega t dt = \frac{2}{\omega} \int_0^{2\pi/\omega} f(t) \cos n\omega t dt \quad \dots\dots\dots(1.4)$$

$$b_n = \frac{1}{\omega} \int_0^{2\pi/\omega} f(t) \sin n\omega t dt = \frac{2}{\omega} \int_0^{2\pi/\omega} f(t) \sin n\omega t dt \quad \dots\dots\dots(1.5)$$

The physical interpretation of Equation (1.1) is that any periodic function can be represented as sum of harmonic functions. Though the series in an infinite sum one can approximate most periodic functions with the help of only a few harmonic function

```
%=====
%
%Program4.m
%Main program which calls PERIOD
%
%=====
%Run "Program4" in MATLAB command window. Program4.m and period.m
%should be in the same folder, and set the path to this folder
%following seven lines contain problem-dependent data
clc
clear all
xm=100.0;
xk=100000.0;
xai=0.1;
n=21;
m=20;
time=0.12;
f=[0.880000    1034.760000    2067.790000    3101.440000    4 1 3 3 . 7 1 2 0 0 0
5219.330000    6202.000000    0.560000...
0.504000    0.308000    0.000000    -0.308000    - 0 . 5 0 4 0 0 0
0.000000    0.000000    0.000000...
0.000000    0.000000    0.000000    0.000000    0.000000];
t=[0.000000    11.110000    22.220000    33.330000    44.330000    55.550000...
66.660000    72.215000    80.540000    88.880000    97.210000    105.545000...
113.870000    122.210000    133.320000    144.430000    155.540000    166.650000...
177.760000    188.870000    200.000000 ];
%end of problem-dependent data
```



```
[phi,fzero,x,xpc,xps]= period(xm,xk,xai,n,m,time,f,t);
fprintf('Response of a single D.O.F. system under periodic force\n\n');
fprintf('xm = %10.8e\n',xm);
fprintf('xk = %10.8e\n',xk);
fprintf('xai = %10.8e\n',xai);
fprintf('n = %2.0f\n',n);
fprintf('m = %2.0f\n',m);
fprintf('time = %10.8e\n\n',time);
fprintf('Applied force and response: \n\n');
fprintf(' i      t(i)      f(i)      x(i)');
fprintf('\n\n');
for i=1:21
    fprintf(' %2.0f      %10.8e      %10.8e      %10.8e\n',i,t(i),f(i),x(i));
end
figure(1)
subplot(121);
plot(t,f);
xlabel('t');
ylabel('F(t)');
title('Program 4: F(t)');
subplot(122);
plot(t,x);
title('Program 4: x(t)');
xlabel('t');
ylabel('x(t)');
```

ANGLE(θ)	FORCE F2 (3)	TIME
0°	0.88	0
20°	1034.76	11.11
40°	2067.79	22.22
60°	3101.44	33.33
80°	4133.712	44.44
100°	5168.536	55.55
120°	6202	66.66
130°	0.56	72.215
145°	0.5243	80.54
160°	0.3631	88.88
175°	0.0	97.21
190°	-0.3856	105.545
205°	-0.5561	113.87
220°	0.16	122.21
240°	0	133.32
260°	0	144.43
280°	0	155.54
300°	0	166.65
320°	0	177.76
340°	0	188.87
360°	0	200

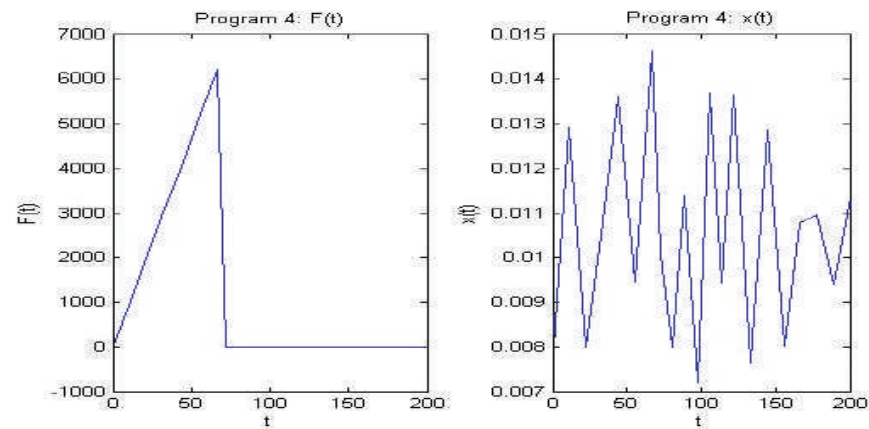


figure 2.2: Schematics of force pattern and corresponding vibration response of follower.

DISCUSSION OF RESULTS

This chapter deals with the result and discussion of the present work. The vibration response obtained by applying a time variant force is discussed phase wise in forthcoming article.

Phase A1-A2:

In this phase ,the force on follower changes from 0.88 kgf to 1034.76 kgf . While the displacement value at point A1 is 0.0088 mm and the displacement value at point A2 is 0.0129 mm. during this section the increment in displacement is seen.

Phase A2-A3:

In this phase ,the force on follower changes from 1034.76 kgf to 2067.79 kgf . While the displacement value at point A2 is 0.0129 mm and the displacement value at point A3 is 0.008 mm during this section the decrement in displacement is seen.

Phase A3-A4:

In this phase ,the force on follower changes from 2067.79 kgf to 3101.44 kgf . While the displacement value at point A3 is 0.008 mm and the displacement value at point A4 is 0.0135 mm during this section the increment in displacement is seen.

Phase A4-A5

In this phase ,the force on follower changes from 3101.44 kgf to 4133.712 kgf . While the displacement value at point A4 is 0.0135 mm and the displacement value at point A5 is 0.0095 mm during this section the decrement in displacement is seen.

Phase A5-A6

In this phase ,the force on follower changes from 4133.712 kgf to 5219.33 kgf . While the displacement value at point A5 is 0.0095 mm and the displacement value at point A6 is 0.0147 mm during this section the increment in displacement is seen.

Phase A6-A7

In this phase ,the force on follower changes from 5219.33 kgf to 6202 kgf . While the displacement value at point A6 is 0.0147 mm and the displacement value at point A7 is 0.008 mm during this section the decrement in displacement is seen.

Phase A7-A8

In this phase the force on a cam and follower changes from 6202 kgf to 0.56 kgf . While the displacement value at point A7 is 0.008 mm and the displacement value at point A8 is 0.0114 mm during this section the increment in displacement is seen.

Phase A8-A9

In this phase ,the force on follower changes from 0.56 kgf to 0.504 kgf . While the displacement value at point A8 is 0.0114 mm and the displacement value at point A9 is 0.0072 mm during this section the decrement in displacement is seen.

Phase A9-A10

In this phase ,the force on follower changes from 0.504 kgf to 0.308 kgf . While the displacement value at point A9 is 0.0072 mm and the displacement value at point A10 is 0.0135 mm during this section the increment in displacement is seen.

Phase A10-A11

In this phase ,the force on follower changes from 0.308 kgf to 0.0 kgf . While the displacement value at point A10 is 0.0135 mm and the displacement value at point A11 is 0.0095 mm during this section the decrement in displacement is seen.

Phase A11-A12

In this phase ,the force on follower changes from 0.0 kgf to -0.308 kgf . While the displacement value at point A11 is 0.0095 mm and the displacement value at point A12 is 0.00134 mm during this section the increment in displacement is seen.

Phase A12-A13

In this phase ,the force on follower changes from -0.308 kgf to -0.504 kgf . While the displacement value at point A12 is 0.0134 mm and the displacement value at point A13 is 0.0076 mm during this section the decrement in displacement is seen.

Phase A13-A14

In this phase ,the force on follower changes from -0.504 kgf to -0.0 kgf . While the displacement value at point A13 is 0.0076 mm and the displacement value at point A14 is 0.0128 mm during this section the increment in displacement is seen.

Phase A14-A15

In this phase ,the force on follower changes from -0.0 kgf to 0.0 kgf . While the displacement value at point A14 is 0.0128 mm and the displacement value at point A15 is 0.0081 mm during this section the decrement in displacement is seen.

Phase A15-A16

In this phase ,the force on follower changes from 0.0 kgf to 0.0 kgf .While the displacement value at point A15 is 0.0081 mm and the displacement value at point A16 is 0.0106 mm during this section the increment in displacement is seen.

Phase A16-A17

In this phase ,the force on follower changes from 0.0 kgf to 0.0 kgf .While the displacement value at point A16 is 0.0106 mm and the displacement value at point A17 is 0.0108 mm during this section the decrement in displacement is seen.

Phase A17-A18

In this phase ,the force on follower changes from 0.0 kgf to 0.0 kgf .While the displacement value at point A17 is 0.0108 mm and the displacement value at point A18 is 0.0094 mm during this section the decrement in displacement is seen.

Phase A18-A19

In this phase ,the force on follower changes from 0.0 kgf to 0.0 kgf .While the displacement value at point A18 is 0.0094 mm and the displacement value at point A19 is 0.011 mm during this section the increment in displacement is seen.

Phase A19-A20

In this phase ,the force on follower changes from 0.0 kgf to 0.0 kgf .While the displacement value at point A19 is 0.011 mm and the displacement value at point A20 is 0.012mm during this section the increment in displacement is seen.

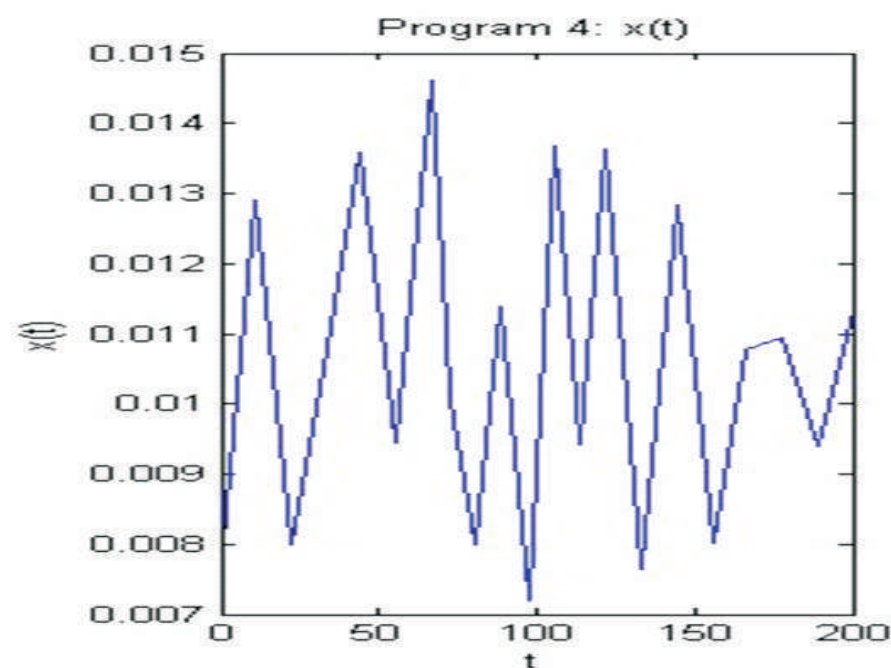


Figure 5.1: Schematic of a vibration response of a follower

CONCLUSION

Through the present investigation following are some important conclusions are made, which are discussed below.

- 1) Considering the present case study, the force pattern is estimated. Which shows linearity for outstroke phase and suddenly falls in return stroke phase.
- 2) The pattern of vibration response of follower shows a periodic vibrations.
- 3) The vibration response of follower shows maximum amplitude is obtained at 0.0147 mm, which occurs at a time 66.66 milisec. The corresponding force is obtained as 6202 kgf. for this maximum amplitude.
- 4) The vibration response of follower shows minimum amplitude is obtained at 0.0072 mm, which occurs at a time 80.54 milisec. The corresponding force is obtained as 0.504 kgf. for this minimum amplitude.

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